

SHOW YOUR WORK FOR FULL CREDIT.

1. Simplify the expression as much as possible.

$$\begin{aligned} \text{(a) } \sin \alpha \tan \alpha + \cos \alpha &= \sin \alpha \frac{\sin \alpha}{\cos \alpha} + \frac{\cos^2 \alpha}{\cos \alpha} \\ &= \frac{\sin^2 \alpha + \cos^2 \alpha}{\cos \alpha} = \frac{1}{\cos \alpha} = \sec \alpha \end{aligned}$$

$$\text{(b) } \frac{\cos^2 x - 4}{\cos x - 2} = \frac{(\cos x + 2)(\cos x - 2)}{\cos x - 2} = \cos x + 2$$

$$\begin{aligned} \text{(c) } \frac{1}{1 + \cos x} + \frac{1}{1 - \cos x} &= \frac{(1 - \cos x) + (1 + \cos x)}{(1 - \cos x)(1 + \cos x)} = \frac{2}{1 - \cos^2 x} \\ &= \frac{2}{\sin^2 x} = 2 \csc^2 x \end{aligned}$$

2. Verify the identity.

$$\text{(a) } \cos^2 x - \sin^2 x = 1 - 2 \sin^2 x$$

$$\cos^2 x - \sin^2 x = (1 - \sin^2 x) - \sin^2 x = 1 - 2 \sin^2 x$$

$$\text{(b) } \frac{1}{\sec \theta \tan \theta} = \csc \theta - \sin \theta$$

$$\frac{1}{\sec \theta \tan \theta} = \cos \theta \cot \theta = \cos \theta \frac{\cos \theta}{\sin \theta}$$

$$= \frac{\cos^2 \theta}{\sin \theta} = \frac{1 - \sin^2 \theta}{\sin \theta}$$

$$= \frac{1}{\sin \theta} - \sin \theta = \csc \theta - \sin \theta$$